

A new strategy for the synthesis of monomethylhydrazine using the Raschig process. 2: Continuous synthesis of stoichiometric monochloramine using the microreactor technology

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Abstract

After having established in a previous paper that the synthesis of stoichiometric monochloramine is hazardous due to the high exothermicity of the reaction and the risk of decomposition of the solution from 36 °C, it appeared that the best solution for this synthesis is to use microreactor technology. A series of experiments carried out using a Doehlert experimental design provided access to a mathematical model describing, for an initial fixed composition ratio $[NH4^+]_0/[OC1^-]_0$, the evolution of the yield as a function of temperature, the flow rate of the reagents and the number of sodium hydroxide equivalent. Thus, the optimal conditions for the synthesis of stoichiometric chloramine using microreactor technology were established.

Keywords Monochloramine · Microreactor · Raschig process · Experimental design

Introduction

In the first part of our study already published [1], we concluded that given the instability of stoichiometric monochloramine solutions from 36 °C and in order to control heat exchanges, the microreactor technology will be the best choice to avoid any sudden degradation leading to the formation of nitrogen chloride NCl₃. Thus, this second part studies the optimal conditions for the synthesis of stoichiometric monochloramine using microreactor technology.

The development of miniaturized systems, known as "microsystems", has progressed considerably over the past 20 years [2, 3]. More recently, these technologies have stimulated the development of microreactors in the field of process engineering

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and industries with chemical-related problems. With regard to the synthesis of monochloramine under stoichiometric conditions, we know that it is highly exothermic and can easily lead to the formation of explosive by-products (NCl₃). Continuous synthesis with current laboratory equipment therefore presents significant risks. For this reason, glass microreactors were used. They will permit the study of this continuous synthesis by limiting the exothermicity of the reaction.

Advantages and limitations

Advantages of microreactors

A fundamental property of the microreactor is the high value of the ratio between its surface area and its volume (specific surface area). For example, this value for the Corning microreactor pilot unit used in this study is $2500 \text{ m}^2/\text{m}^3$, with channels with a hydraulic diameter of 0.7 mm. Wall phenomena are thus intensified. In particular, heat transfer is significantly increased compared to the other type of reactors [4]. Table 1 shows, for example, a comparison between different reactor types.

These transfer characteristics allow for better control and accuracy of operating conditions compared to conventional reactors. In addition, parasitic reactions can be avoided by operating within a narrow window of parameters where the best selectivity is found.

The small dimensions of the microreactor system are also of interest, mainly in terms of safety, due to the very small volume of product handled. This is a considerable advantage for the maintenance and management of safety in processes involving high-risk compounds (explosive, toxic).

Glass microreactors allow easy visualization of phenomena and improved chemical resistance. In general, glass is an excellent material for water, salt solutions, acids and organic compounds [5].

In industrial production, micro-reactors make it possible to avoid scale-up operations. The transition from laboratory experiment scale to industrial scale essentially consists in parallelizing the units (numbering-up). This method makes it possible to avoid the heavy assumptions about extrapolation factors as well as the risks intrinsic to any change in scale (degradation of product quality, loss of energy performance, hydrodynamic dysfunctions, etc.) [4].

Limits of microreactors

Microreactors are limited by the laws of hydrodynamics. Indeed, the miniaturization of the channels inevitably leads to an increase in pressure drop. In order to compensate this pressure drop, it is necessary to work under pressure to have a sufficient flow in the channels. On the laboratory microreactor unit, the pressure is in the range of 7–10 bar for flows ranging from 80 to 120 mL min⁻¹. On the other hand, glass remains very fragile in the face of mechanical stresses and strains. Synthesis

Module	Specific area m ² /m ³	Volumetric thermal transfer coefficient MW/m ³ K
Batch reactor	2.5	10 ⁻³
Batch reactor with exchanger	10	10 ⁻²
Tubular exchanger	400	0.2
Plate heat exchanger	800	1.25
Glass Corning microstructure	2500	1.7

 Table 1 Comparison table of current exchange modules [12]

is therefore limited to pressures below 20 bar with a maximum total flow rate of 200 mL min^{-1} .

For continuous use of microreactors at the industrial level, the passage of reagents will lead to progressive fouling of the microchannels. They will therefore have a limited operating time, which will vary depending on the reagents used and the products formed during the synthesis. This pollution will therefore require a special cleaning protocol and, possibly in the long term, a replacement cycle for microreactor modules.

Experimental part

Corning microreactor

The study of the continuous synthesis of stoichiometric monochloramine was performed on the Corning microreactor unit shown in Fig. 1.

The different elements of the Corning microreactor unit are as follows:

- 2 DTR microstructures: pre-cooling plates,
- 1 MFA microstructure: separation of the bleach supply into 4 streams,
- 1 MJ microstructure: reaction plate composed of 4 mixing zones.

For each structure, the experimental conditions are as follows:

DTR microstructure: $V_{reagent}$: 9 mL, $V_{heat exchange}$: 14 mL, $S_{exchange}$: 17,500 mm², ΔP : 100 mbar MFA microstructure: $V_{reagent}$: 1 mL, $V_{heat exchange}$: 13 mL, $S_{exchange}$: 3000 mm² MJ microstructure: $V_{reagent}$: 10 mL, $V_{heat exchange}$: 16 mL, $S_{exchange}$: 23,500 mm², ΔP : 2500 mbar with: $S_{exchange}$: heat exchange surface of the microstructure (mm²) and ΔP : pressure drop in the microstructure (mbar) (Pressure drops are measured with water at a flow rate of 100 mL min⁻¹ and at 20 °C).

The so-called "microreactor" part is composed of 4 glass modules. The 2 DTR modules are designed to pre-cool the reagents at different temperatures. The MFA module is a manifold that divides the bleach supply into 4 streams of equal flow rates.



Fig. 1 Diagram of the Corning microreactor pilot unit

The MJ module is the reaction module with 4 mixing zones. It provides mixing and residence time actions at each injection point. The hydraulic diameter of the channels in the glass modules is 0.7 mm (manufacturer's data). The fluid flow regime in the microreactor unit is therefore laminar (Reynolds number is less than 10^4).

In order to overcome the laminar regime, obstacles are created in the MJ microstructure plate (Fig. 2). These obstacles aim to break the flow and create a turbulent flow, which means better heat exchange and better mixing action.

Temperature control is provided by Lauda Integral T 2200 thermostats with 2.7 kW cryogenic power. They allow working in a temperature range from -25 to 120 °C. Reagent flow is controlled with two HNP Mikrosysteme Mzr-7259Ex gear pumps (PP1, PP2) and two ROTAMASS series 3 Coriolis mass flowmeters (FM1, FM2) supplied by Yokogawa. Sensors T1, T2, T3 and P1, P2, P3 are used to monitor the temperature and pressure of the fluids before and after reaction, as well as the system pressure drops as a function of the fluid flows.

Chemical products

The permuted water used is city water purified by passing over an ion exchange resin. The inorganic salts and organic solvents used are of commercial purity (minimum 98%) and are supplied by Acros Organics, Merck and Sigma-Aldrich. They were used without prior purification unless otherwise indicated. Aqueous solutions of sodium hypochlorite NaOCl and sodium hydroxide are supplied by Arkema (Jarrie Plant, Grenoble, France). The aqueous solution, measuring approximately 48 chlorometric degrees (2.4 mol L⁻¹), is stored at 5 °C and systematically titrated before use.

Analytical methods

lodometric dosage

This method was used to determine the active chlorine concentrations of chloramine solutions and hypochlorite ions. It is based on the oxidation of potassium iodide in acetic medium with titration of iodine released by a 0.1 M sodium thiosulfate solution. The dosing reaction was monitored by potentiometry using a Metrohm 6.0451.100 combined platinum electrode.



Fig. 2 Structure created in the MJ microstructure unit to break the flow

UV spectrometry

The spectrophotometer used was an Agilent Cary 100 dual beam spectrophotometer equipped with the Cary WinUV data acquisition system. It allows a repetitive scanning of spectra between 180 and 900 nm, programmable as a function of time, and measurements of optical density or its derivatives at a given wavelength. Measurements were made with Hellma® brand Suprasil® quartz cells, model 100-QS with a 10 mm optical path, to ensure optimal transmission of UV signals.

Continuous chloramine synthesis

Between two manipulations, an isopropanol solution is injected into the device to ensure proper preservation of the pumps and glass microstructures. The rinsing solution used to purge and clean the installation is then a mixture of 25% water and 75% ethanol.

The reagent solutions (NH₄Cl solution and alkaline bleach solution) are previously prepared and cooled (generally -5 °C). Before each synthesis experiment, a water/ethanol solution is circulated at the desired flow rate to remove isopropanol from the pipes. Once the isopropanol has been purged, NH₄Cl is introduced and then bleach. The synthesis is carried out, for all experiments, under a pressure of 11 bar. During normal operation, the steady state is reached after 10 min. Samples are then taken punctually, every 15 min, then analyzed by iodometric dosage and UV–Visible spectrometry. Measurements of temperature, fluid density and pressure are carried out online at different points in the installation in order to check that the synthesis is proceeding correctly and to make an immediate correction in the event of significant deviations from the instructions. A pH monitoring at the end of the reaction module is necessary to avoid any drift of the monochloramine solutions. Indeed, a pH below 10 leads to the potential formation of highly explosive dichloramine NHCl₂ and nitrogen trichloride NCl₃.

At the end of the synthesis, the microreactor unit is rinsed with a water/ethanol solution for 30 min, then an isopropanol solution is injected to preserve the pumps and microstructures.

Results and discussion

Experimental design

Experimental design method

Throughout this study on the Corning microreactor unit, many parameters that could influence the synthesis were investigated. The classical experimental methodology consists of setting the level of all but one of the variables and measuring the system response for different values of this variable, which implies carrying out a considerable number of experiments. For example, for 4 variables at 4 levels (i.e. using 4 different values for each variable), $4^4 = 256$ experiments must be performed. In order to avoid too many experiments, the design of experiments method was used.

Indeed, the designs of experiments are derived from mathematical and statistical methods applied to experimentation. The principle of this technique is to simultaneously vary the levels of one or more factors (discrete or continuous variables) in each experiment. This will significantly reduce the number of experiments to be carried out while increasing the number of factors studied, detecting the interactions between the different factors and a given response, i.e. a quantity used as a criterion, and allowing the results to be modelled. It should be noted that the main difference with the traditional method is that the design of experiments method allows the levels of all factors to be varied at the same time for each experiment, in a programmed and reasoned way [6].

For this study, the factors studied were:

- the number of soda equivalent in bleach,
- the temperature of the reagents (bleach and NH₄Cl solution),
- the flow of fluids,
- the pressure.

Complete factorial plan 2³

First, the most influential factors governing the system response will be sought rather than a specific relationship between factor variations and response variations. Previous studies in the laboratory have shown a significant influence of the amount of soda present in bleach on the monochloramine yield of the synthesis [7]. The influence of the remaining three factors (temperature, flow and pressure) therefore remains to be quantified.

To this end, a complete factorial design with these three factors (temperature, flow rate and pressure) was used, due to its simplicity and speed of implementation. This method consists of performing the experiments by varying the factors between a high (+) and low (-) level. In this case, this plan is rated 2³ (3 factors with 2 levels each), and therefore includes 8 experiments. The numerical values of the 2 levels of each of the 3 factors and the associated response (monochloramine yield) are given in Table 2.

The mathematical model associated with the complete plan 2^3 is as follows:

$$y = a_0 + a_1 x_1 + a_2 x_2 + a_3 x_3 + a_{12} x_1 x_2 + a_{13} x_1 x_3 + a_{23} x_2 x_3 + a_{123} x_1 x_2 x_3$$

with: y: the answer (in this case, the yield of the synthesis), x_i : the abscissa of the experimental point for factor i. Given the levels that the factors take, x_i takes the value 1 for level (+) and -1 for level (-), a_0 : the value of the response at the center of the field of study, a_i : the effect of factor i, a_{ij} : the interaction between factors i and j (the same for a_{123} which is the interaction between the three factors).

The coefficients of the model can be determined using the following matrix equation:

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Experiment number	Factor 1 Temperature	Factor 2 Flow rate	Factor 3 Pressure	Answer NH ₂ Cl Yield (%)
	Temperature	1 low fute	Tressure	
1	+	+	+	86.9
2	-	+	+	99.0
3	+	-	+	86.0
4	+	+	_	92.6
5	_	_	+	99.5
6	_	+	_	99.0
7	+	_	_	83.2
8	-	-	-	98.6
Effective values		°C	$mL min^{-1}$	Bar
Level (+)		30	100	16
Level (-)		- 10	30	7

 Table 2
 Plan 2³ experience Matrix, summary of the experiments

$[Y_1]$		[+1 +1 +1 +1 +1 +1 +1 +1]		a ₀ –
Y_2		+1 -1 +1 +1 -1 -1 +1 -1		a ₁
Y ₃		+1 $+1$ -1 $+1$ -1 $+1$ -1 -1		a ₂
Y_4	_	+1 $+1$ $+1$ -1 $+1$ -1 -1 -1		a ₃
Y_5	=	+1 -1 -1 +1 +1 -1 -1 +1	•	a ₁₂
Y ₆		+1 -1 +1 -1 -1 +1 -1 +1		a ₁₃
Y ₇		+1 $+1$ -1 -1 -1 -1 $+1$ $+1$		a ₂₃
Y ₈		+1 -1 -1 -1 +1 +1 +1 -1		a ₁₂₃

then, in condensed form:

 $\mathbf{y} = \mathbf{X} \cdot \mathbf{a}$

with: **y**: column matrix containing the eight answers, **X**: effects calculation matrix. This matrix is composed of the values taken by the levels of different factors or the products of the coordinates of these factors [8], **a**: column matrix of the coefficients of the mathematical model.

The values of the coefficients of the model are obtained by solving the matrix equation.

$$\begin{bmatrix} a_0 \\ a_1 \\ a_2 \\ a_3 \\ a_{12} \\ a_{13} \\ a_{23} \\ a_{123} \end{bmatrix} = \mathbf{a} = \mathbf{X}^{-1} \cdot \mathbf{y} = \begin{bmatrix} 93.49 \\ -5.54 \\ 1.66 \\ 0.14 \\ 1.69 \\ -0.09 \\ -0.79 \\ -0.56 \end{bmatrix}$$

The effects of the different factors and their interactions are shown in Fig. 3.



Fig. 3 Coefficients of the mathematical model of the plan 2^3

To conclude, Fig. 3 shows that among these three factors, the most influential are, in order of importance, temperature and flow rate. Pressure is not a decisive parameter. These factors will now be addressed in a Doehlert plan.

Composite plan of Doehlert

The combination of all the results shows that the factors that have the most influence on the yield of monochloramine synthesis are: the amount of NaOH in bleach, temperature and fluid flow. Pressure has very little influence and is therefore now set for all experiments at 11 bar, a value similar to that of the installations at the industrial ArianeGroup site in Toulouse (France).

In order to study the effects of these three factors on performance, a Doehlert plan of experiments is established, because of its advantages over factor designs. The first advantage of Doehlert plan is that each factor now has several levels (instead of 2 as in factorial plan 2³). The number of levels for each factor is variable, which allows the operator flexibility to assign a large number of levels or not to a factor. In this study, the "number of soda equivalent" factor was chosen as the factor with the highest number of levels, in order to obtain the maximum information from the system. Finally, the representative points of the different experiments in the Doehlert plan are placed according to a geometric figure, which ensures that the experiments are regularly placed in the experimental space [8]. Fig. 4 shows, schematically, the distribution of experiments for a three-factor Doehlert plan.

The postulated mathematical model used with Doehlert plan is a second degree equation:

$$y = a_0 + a_1 x_1 + a_2 x_2 + a_3 x_3 + a_{12} x_1 x_2 + a_{13} x_1 x_3 + a_{23} x_2 x_3 + a_{11} x_1^2 + a_{22} x_2^2 + a_{33} x_3^2$$





with: y: the answer (in our case, the yield of the synthesis), x_i : the abscissa of the experimental point for factor i in coded coordinates (Table 3), a_i , a_{ij} : coefficient of the mathematical model.

Experiment	Factor 1		Factor 2		Factor 3	
number	Temperature		Soda equivalent		Flow rate	
	Encoded value	Real value (°C)	Encoded value	Real value	Encoded value	Real value (mL min ⁻¹)
1	0	8	0	0.26	0	60
2	1	24	0	0.26	0	60
3	0.5	16	0.866	0.47	0	60
4	- 0.5	0	- 0.866	0.05	0	60
5	- 1	- 8	0	0.26	0	60
6	- 0.5	0	- 0.866	0.05	0	60
7	0.5	16	- 0.866	0.05	0	60
8	0	8	0	0.26	0	60
9	- 0.5	0	0.289	0.33	0.816	80
10	0	8	- 0.577	0.12	0.816	80
11	0.5	16	0.289	0.33	0.816	80
12	-0.5	0	- 0.289	0.19	- 0.816	40
13	0	8	0.577	0.40	- 0.816	40
14	0.5	16	- 0.289	0.19	- 0.816	40
15	0	8	0	0.26	0	60
Level – 1		- 8		0.02		35
Level 0		8		0.26		60
Level + 1		24		0.50		85

 Table 3
 Doehlert plan for three factors, summary of experimental tests

N.B. : $0.866 = \frac{\sqrt{3}}{2}; 0.816 = \frac{\sqrt{2}}{\sqrt{3}}; 0.577 = \frac{1}{\sqrt{3}}; 0.289 = \frac{1}{2\sqrt{3}}$

The parameters of the plan experiments and the experimental results are shown in Table 3:

In this case, the calculation matrix is a 15×10 matrix since there are 15 experiments and 10 coefficients in the mathematical model. These coefficients are calculated by the following formula[8]:

$$\mathbf{a} = (\mathbf{X}^{\mathrm{T}} \cdot \mathbf{X})^{-1} \cdot \mathbf{X}^{\mathrm{T}} \cdot \mathbf{y}$$

with: a: vector of coefficients, X: calculation matrix $(X^{T}: matrix transposed from X)$, y: vector of experiment results.

After solving the matrix equation, the mathematical model is as follows:

$$y = 97.73 - 1.642x_1 - 4.003x_2 - 3.505x_3 + 39.193x_1x_2$$

-12.883x_1x_3 - 6.568x_2x_3 + 0.030x_1^2 - 40.578x_2^2 - 4.770x_3^2

Table 4 shows the experimental and modelled results for each experiment performed.

The overall quality of the adjusted mathematical model is assessed using the following two statistical tools [9]:

Fisher test

This test aims to reject the hypothesis (H_0) that the model does not describe the variation of the tests. When this hypothesis is verified, it is shown that the statistic $F_{regression}$, described by the relationship below, follows a Fisher law with, v_X and v_R

Table 4 Results of the Doehlert plan experiments	Experiment number	Experimental yield (%)	Modelled yield (%)
	1	97.73	97.73
	2	99.96	99.40
	3	83.38	81.63
	4	84.19	86.92
	5	95.56	96.12
	6	87.9	86.92
	7	54.62	54.62
	8	97.73	97.73
	9	84.95	84.39
	10	85.32	83.57
	11	84.52	86.83
	12	95.53	93.22
	13	82.92	84.67
	14	93.51	94.07
	15	97.73	97.73

degrees of freedom [10]. v_X and v_R are the numbers of degrees of freedom associated, respectively, with the sum of the squares of deviations from the regression average value and the sum of the squares of the residues.

$$F_{regression} = \frac{\sum (\hat{y_i} - \overline{y})^2}{\sum (y_i - \hat{y_i})^2}$$

with: \overline{y} average value of experimental results, y_i : experimental value for experiment number i, $\hat{y_i}$: value calculated from the model for experiment number i.

Thus, this hypothesis is rejected with a probability α if

$$F_{\text{regression}} > F(\alpha; v_X; v_R)$$

Here $F(\alpha; v_X; v_R)$ is the $(1 - \alpha)$ quantile of a Fisher law with v_X and v_R degrees of freedom.

Coefficient of determination R² of the multilinear regression

This coefficient is defined by the ratio of the dispersion of the results, explained by the model, to the total dispersion of the results:

$$\mathbf{R}^{2} = \frac{\sum \left(\widehat{\mathbf{y}}_{i} - \overline{\mathbf{y}}\right)^{2}}{\sum \left(\mathbf{y}_{i} - \overline{\mathbf{y}}\right)^{2}}$$

When $R^2 = 1$, the estimations by the mathematical model coincide with the measurements, while for $R^2 = 0$, the data are not at all aligned. The value of R^2 , in this case, is 0.98, which means that 98% of the variation in the experiments is explained by the mathematical model.

The experimental results lead to Table 5.

According to Table 5, the statistic $F_{regression}$ satisfies the Fisher test with a 95% confidence level. This mathematical model therefore makes it possible to describe the response of the experiments in a satisfactory way.

Canonical analysis

The mathematical model associated with Doehlert plan is a second order polynomial model, so a canonical analysis can be performed. This technique allows to easily

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Source of variation	Degree of liberty	Sum of the squares	Expression	F _{regression}	F(0.95; 9; 5)	\mathbb{R}^2
Total	15 – 1	1773.70	$\sum (y_i - \overline{y})^2$	59	4.772	0.98
Regression	10 – 1	1744.20	$\sum (\hat{y_i} - \overline{y})^2$			
residual	15 – 10	29.52	$\sum \left(y_i - \widehat{y_i}\right)^2$			

 Table 5
 Fisher test for regression

deduce the essential characteristics of the model such as: the coordinates of the stationary point of the model and the associated response, the type of the stationary point (maximum, minimum, minimax), the main axes as well as the variation of the model relative to each of these axes [11]. To do this, the mathematical model was written in the following matrix form:

$$\mathbf{y} = \mathbf{a}_0 + \mathbf{x}^{\mathrm{T}} \cdot \mathbf{b} + \mathbf{x}^{\mathrm{T}} \cdot \mathbf{B} \cdot \mathbf{x}$$

with

$$\mathbf{x} = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} \qquad \mathbf{b} = \begin{bmatrix} a_1 \\ a_2 \\ a_3 \end{bmatrix} = \begin{bmatrix} -2.67 \\ 3.69 \\ 0.11 \end{bmatrix}$$
$$\mathbf{B} = \begin{bmatrix} a_{11} & \frac{1}{2}a_{12} & \frac{1}{2}a_{13} \\ \frac{1}{2}a_{12} & a_{22} & \frac{1}{2}a_{23} \\ \frac{1}{2}a_{13} & \frac{1}{2}a_{23} & a_{33} \end{bmatrix} = \begin{bmatrix} -0.47 & 9.84 & -3.92 \\ 9.84 & -26.88 & -4.92 \\ -3.92 & -4.92 & -6.37 \end{bmatrix}$$

The matrix equation of the second degree model implicitly implies the existence of a so-called stationary point S (unique) for which the partial derivatives of the response with respect to variables x_i are all zero. Thus:

$$\frac{\partial y}{\partial \mathbf{x}} = 0$$

which gives:

$$\mathbf{x}_{S} = -\frac{1}{2}\mathbf{B}^{-1} \cdot \mathbf{b}$$
 and $\mathbf{y}_{S} = \mathbf{a}_{0} - \frac{1}{4}\mathbf{b}^{\mathrm{T}} \cdot \mathbf{B}^{-1} \cdot \mathbf{b}$

The stationary point is therefore:

$$x_{S} = \begin{bmatrix} 0.48 \\ -0.21 \\ -0.64 \end{bmatrix} = \begin{bmatrix} \text{temperature} = 15.7 \,^{\circ}\text{C} \\ \text{eq NaOH} = 0.21 \text{ equivalent} \\ \text{flow rate} = 44 \,\text{mL min}^{-1} \end{bmatrix} \text{ and } y_{S} = 102.49$$

A significant simplification can be achieved if the mathematical model is seen from a particular benchmark, translated and returned relative to the original benchmark (factor benchmark x_i). To do this, first of all, the axes of the original reference frame will be rotated around its origin. The purpose of this operation is to remove the interaction monomas between factors x_i . Once the rotation is completed, a translation will allow the removal of the first order terms from the polynomial model. Fig. 5 shows, for example, the position of the axes during these operations.

The objective of this transformation is to bring the model back to the following canonical form:

$$y=y_S+\lambda_1\cdot z_1^2+\lambda_2\cdot z_2^2+\lambda_3\cdot z_3^2$$



Fig. 5 Position of the axes during the transformation operations. **a** original position (original axes); **b** positions of the axes during rotation; **c** position of the axes during translation

with y: the response of the model (in this case, the yield of the synthesis), z_i : the ith coordinates of the experimental point in the final reference frame, y_S : the response at the stationary point S, λ_i : the eigenvalues of matrix B.

To do this, matrix B must be transformed into a diagonal matrix. The notions of vectors and eigenvalues then come into play. We will note Θ the diagonal matrix whose element Θ_{ii} is the eigenvalue λ_i of B.

$$\boldsymbol{\Theta} = \begin{bmatrix} \lambda_1 & 0 & 0 \\ 0 & \lambda_2 & 0 \\ 0 & 0 & \lambda_3 \end{bmatrix}$$

In the final reference frame, the mathematical model will therefore be written in the following matrix form:

$$y = y_{S} + z^{T} \cdot \Theta \cdot z$$

Similarly, the matrix is defined by M for which the ith column is the ith eigenvector of B. This matrix M plays an important role since it allows the passage of the coordinates of the experimental point in the original reference frame $x = [x_1, x_2, x_3]^T$ to the coordinates $z = [z_1, z_2, z_3]^T$ in the final reference frame, and vice-versa:

$$\mathbf{z} = \mathbf{M}^{\mathrm{T}} \cdot \left(\mathbf{x} - \mathbf{x}_{\mathrm{S}}\right)$$

 $\mathbf{x} = \mathbf{x}_{s} + \mathbf{M} \cdot \mathbf{z}$

The numerical results in the case of this mathematical model are presented:

$$\mathbf{\Theta} = \begin{bmatrix} -30.65 & 0 & 0\\ 0 & 5.25 & 0\\ 0 & 0 & -8.32 \end{bmatrix}$$

and M =
$$\begin{bmatrix} 0.2898 & -0.8464 & 0.4467 \\ -0.9461 & -0.3239 & -0.0001 \\ -0.1448 & 0.4226 & 0.8947 \end{bmatrix}$$

The unit vectors of the final reference frame, expressed in coordinates of the original reference frame with their associated eigenvalues, are:

$$z_1 = \begin{bmatrix} 0.2898 \\ -0.9461 \\ -0.1448 \end{bmatrix} \quad z_2 = \begin{bmatrix} -0.8464 \\ -0.3239 \\ 0.4226 \end{bmatrix} \quad z_3 = \begin{bmatrix} 0.4467 \\ -0.0001 \\ 0.8947 \end{bmatrix}$$

The mathematical model is therefore written:

$$y = 98.09 - 48.502 \cdot z_1^2 + 11.195 \cdot z_2^2 - 8.012 \cdot z_3^2$$

Two eigenvalues are negative (λ_1 and λ_3) and one eigenvalue is positive (λ_2) . The response y decreases on axes z_1 and z_3 with negative eigenvalues, but increases on axis z_2 . The order of magnitude of the coefficients is also important. Indeed, for the same variation of the z_i component of z, its effect will be all the greater if the corresponding coefficient (λ_i) is great. On the other hand, this effect will be all the less important if its coefficient is small. Fig. 6 shows the effects of changes of the z_i components.

Fig. 7 visually shows the relative positions of the unit vectors of the original (x_i) and final (z_i) landmarks.

The canonical analysis that has been carried out shows that to increase the response y (the yield of monochloramine synthesis), it is necessary to move away from the stationary point S along the z₂ axis (whose associated eigenvalue λ_2 is positive). 2 points are considered: $P_1 = [0, 1, 0]_{marker z}$ and $P_2 = [0, -1, 0]_{marker z}$ 0]_{marker z}. These two points therefore correspond to the following two experimental conditions:



Fig. 6 Variations of the response y according to the axes z_i



Fig. 7 Relative positions of the unit vectors of the original and final landmarks (views taken from different angles)

$$P_{1} = \begin{bmatrix} 0.36 \\ -0.53 \\ -0.22 \end{bmatrix}_{\text{marker x}} = \begin{bmatrix} \text{temperature} = 2.2 \text{ }^{\circ}\text{C} \\ \text{eqNaOH} = 0.13 \text{ equivalent} \\ \text{flow rate} = 54.6 \text{ mL min}^{-1} \end{bmatrix}$$
$$P_{2} = \begin{bmatrix} 1.33 \\ 0.12 \\ -1.06 \end{bmatrix}_{\text{marker x}} = \begin{bmatrix} \text{temperature} = 29.3 \text{ }^{\circ}\text{C} \\ \text{eqNaOH} = 0.29 \text{ equivalent} \\ \text{flow rate} = 33.5 \text{ mL min}^{-1} \end{bmatrix}$$

Point P_2 is rejected because of its high reagent temperature. This high temperature strongly favours the degradation of the solution and can potentially cause a sudden or even rapid degradation of the synthesis. For safety reasons, point P_1 is adopted as the optimal conditions for the synthesis of stoichiometric chloramine on the microreactor unit.

Conclusion

For the first time, the use of microreactors allows the continuous preparation of stoichiometric monochloramine. Under the experimental conditions studied, the study of the synthesis of NH₂Cl on the microreactor pilot unit allows to conclude that:

- The total flow rate has very little influence on reaction performance,
- Two parameters have a decisive influence on the reaction performance, namely the temperature and the number of sodium equivalent in bleach,
- An excess of sodium hydroxide gradually leads to a drop in the initially almost quantitative yield from 97 to 84%. This is due to a substitution reaction of Cl⁻ by OH⁻ with transient formation of hydroxylamine. The number of sodium equivalent does not exceed 0.25 to obtain a quasi-quantitative yield.

The lower bound of number of sodium equivalent is strongly influenced by temperature. Generally speaking, if the number of sodium equivalent is equal to 0.05, a lower yield at 86% (T=0 °C) is observed which is aggravated by a rise in temperature.

The major safety parameter is the initial concentration of sodium hydroxide in bleach. Whatever the temperature, this parameter must, in all cases, be higher than the minimum of 0.1, preferably for safety reasons at 0.2–0.25. Under these conditions, it is possible to carry out the synthesis preferably between 0 and 24 °C.

To ensure process safety, it would be necessary to continuously measure the pH of the chloramine solution downstream of the reactor and/or perform an online UV measurement to verify the conformity of the absorption spectrum.

After discussion with our industrial partner and taking into account process safety aspects, we therefore recommend the following conditions for the synthesis of stoichiometric monochloramine:

Temperature: 0 °C NaOH equivalent: 0.20 eq Reagent flow rate: 50 mL min⁻¹ Pressure: 11 bar.

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